

Universität Stuttgart, Fakultät Luft- und Raumfahrttechnik und Geodäsie
- Vorlesung -

***Strömungsinstabilitäten
und laminar-turbulenter Strömungsumschlag***

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***Flow Instability and
Laminar-to-Turbulent Transition***

Hauptdiplom, Vertiefungsfach Strömungslehre
2 Semesterwochenstunden im SS

Dozent:
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Snapshot of near-wall vortices in a turbulent boundary layer (top view, after crossflow transition, $Re_{\theta} = 950$).

Upper: *vortices*

(λ_2 -isosurfaces, $y^+ < 100$)

and, in background,

wall-normal vorticity ω_y ($y^+ \approx 6$);

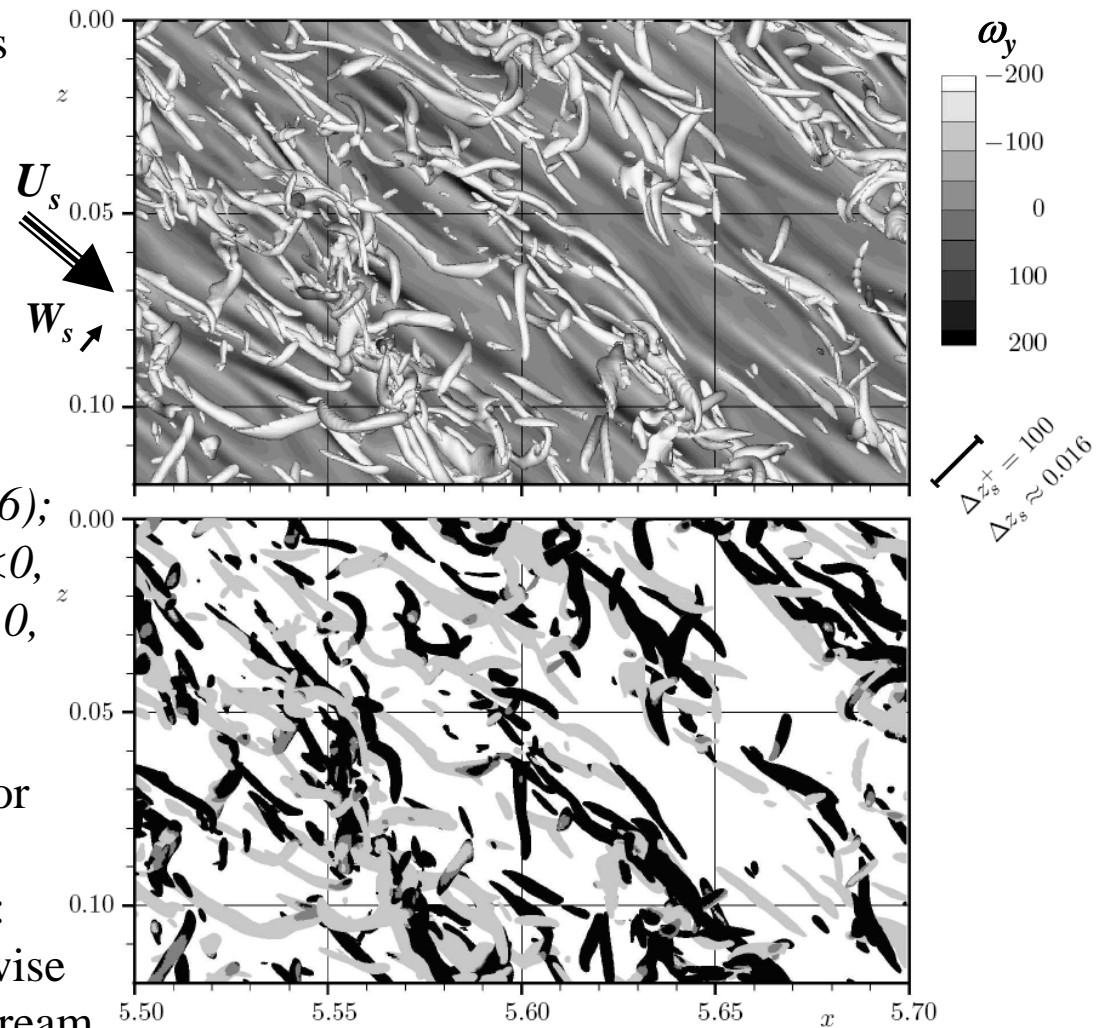
white: *low-speed streaks*, $\omega_y < 0$,

dark: *high-speed streaks*, $\omega_y > 0$, generated by the vortices.

Lower: *streamwise vorticity* for the vortices shown above,

indicating their rotation sense:

black/grey means anti-/clockwise rotation when looking downstream.



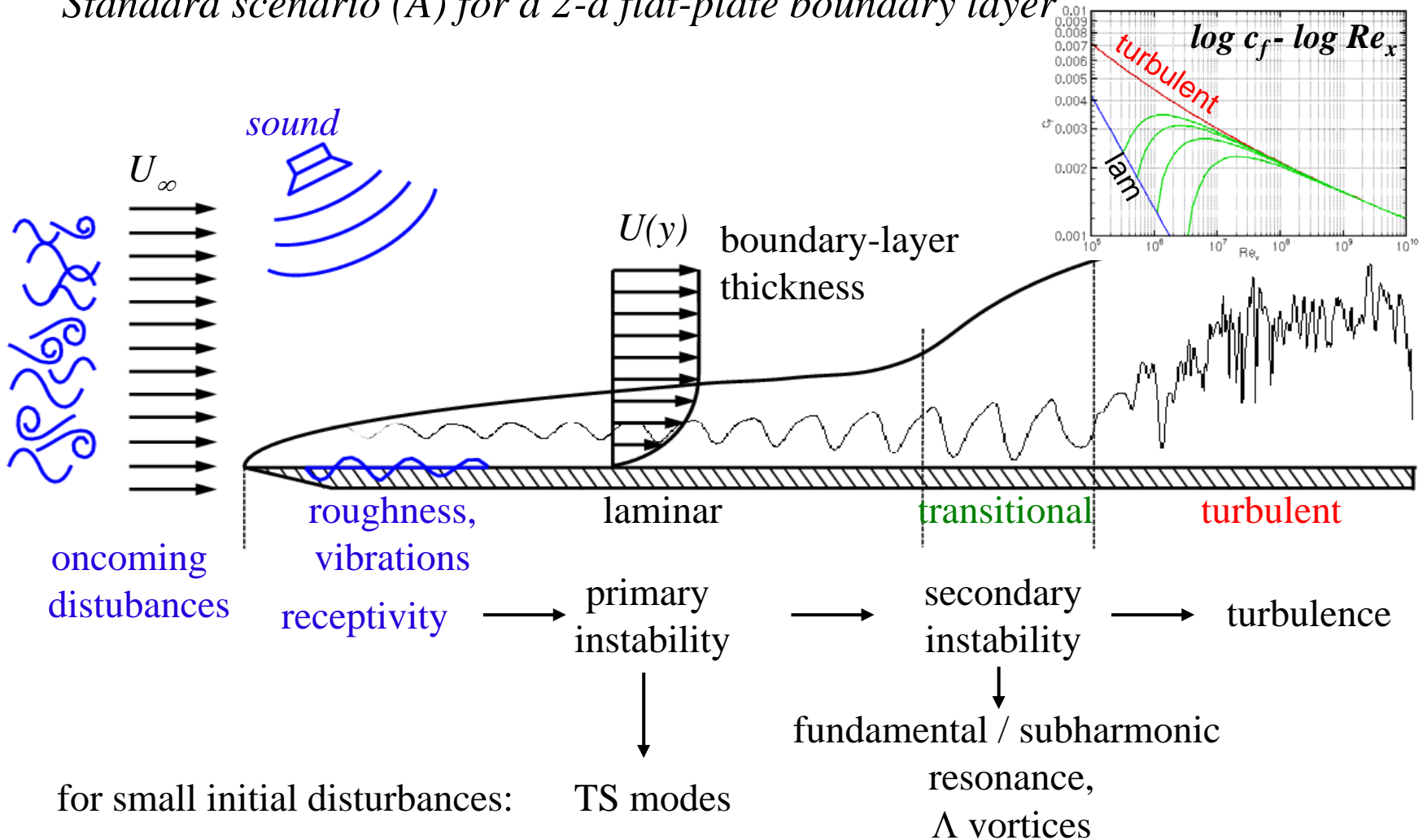
DNS Bonfigli & Kloker, IAG, 2002/6

- Review of the routes to “turbulence”: **any unsteady flow is a consequence of an instability of the underlying steady base flow** if unsteady excitation is small or absent
- Introduction of the concept of (linear) **primary instability** of laminar shear flows:
 - modal exponential disturbance growth of wave-like disturbances
 - Orr-Sommerfeld Equation
 - non-modal, transient growth
- Transition prediction: $exp(N)$ method based on OSE
- Discussion of the influence of, e.g., crossflow velocity, Mach number, wall temperature on the flow instability
- Weakly nonlinear instability: spectral and local **secondary instability**
- Fully nonlinear mechanisms of laminar breakdown with **formation of dynamical structures**
- Examples from experiments and detailed direct numerical simulations
- Discussion of some transition control methods

Scenario A – Basics, 1

Flow Instability

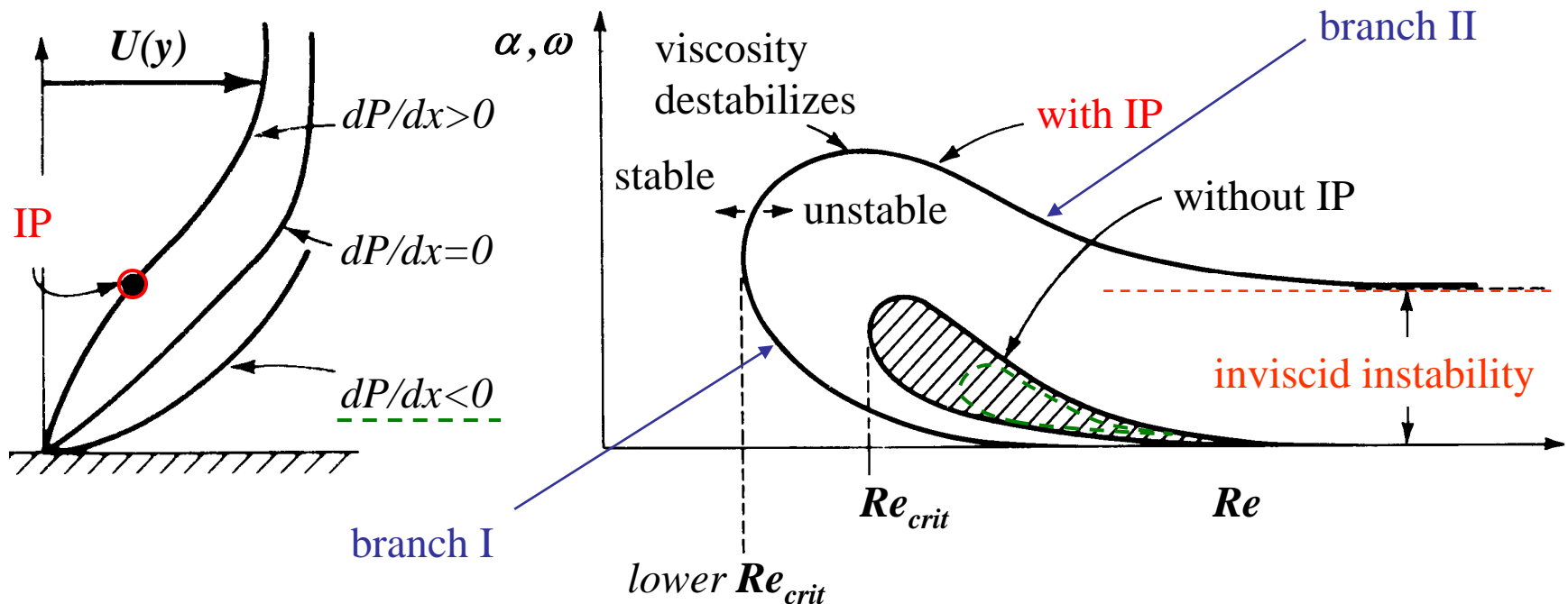
Standard scenario (A) for a 2-d flat-plate boundary layer



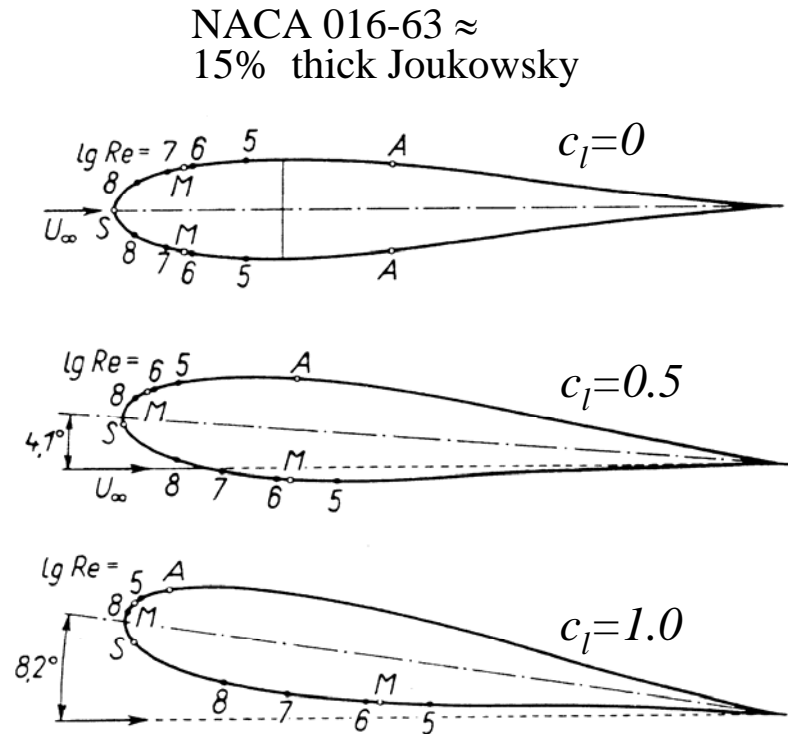
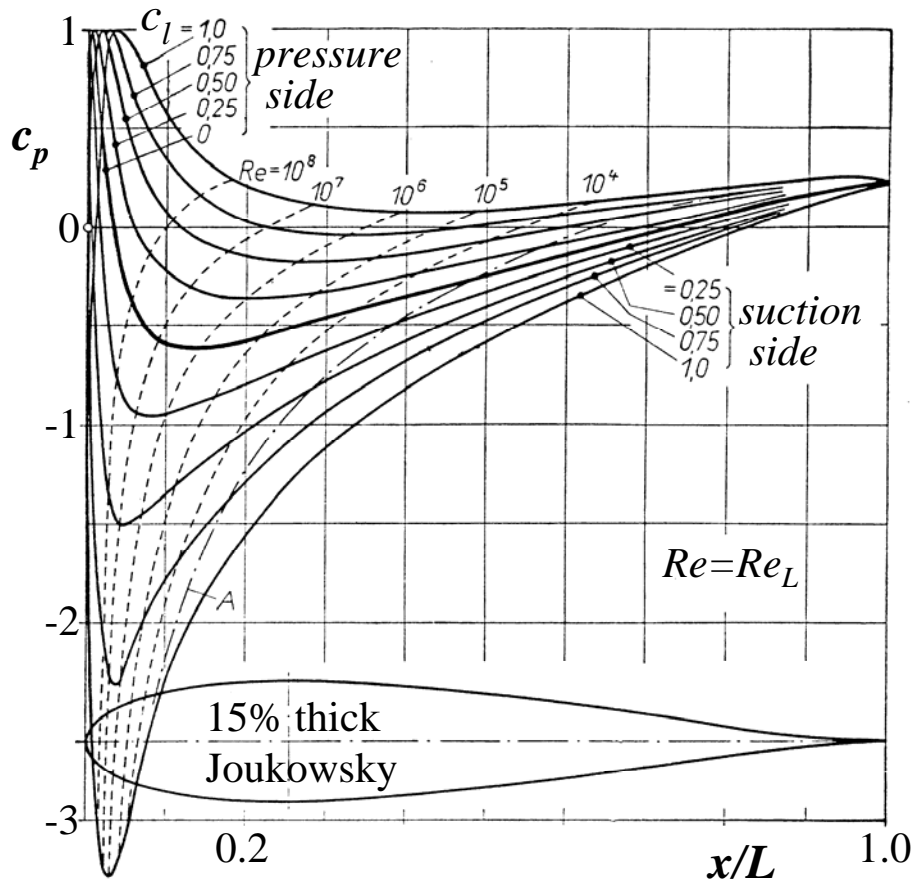
Scenario A – Primary Instability

Flow Instability

- Orr-Sommerfeld equation: TS-waves that represent downstream travelling “infinitely small spanwise vortices” can grow exponentially in a shear flow
- Stability diagram (2-d waves): instability inside “banana”
- Strong “inviscid” instability exists if the base-flow profile $U(y)$ has an inflection point (IP) and at this point the modulus of the spanwise vorticity ($\sim |dU/dy|$) has a maximum as, e.g., for Falkner-Skan profiles with $\beta_H < 0$.



Primary Instability, OSE / experiments, 1 *Flow Instability*

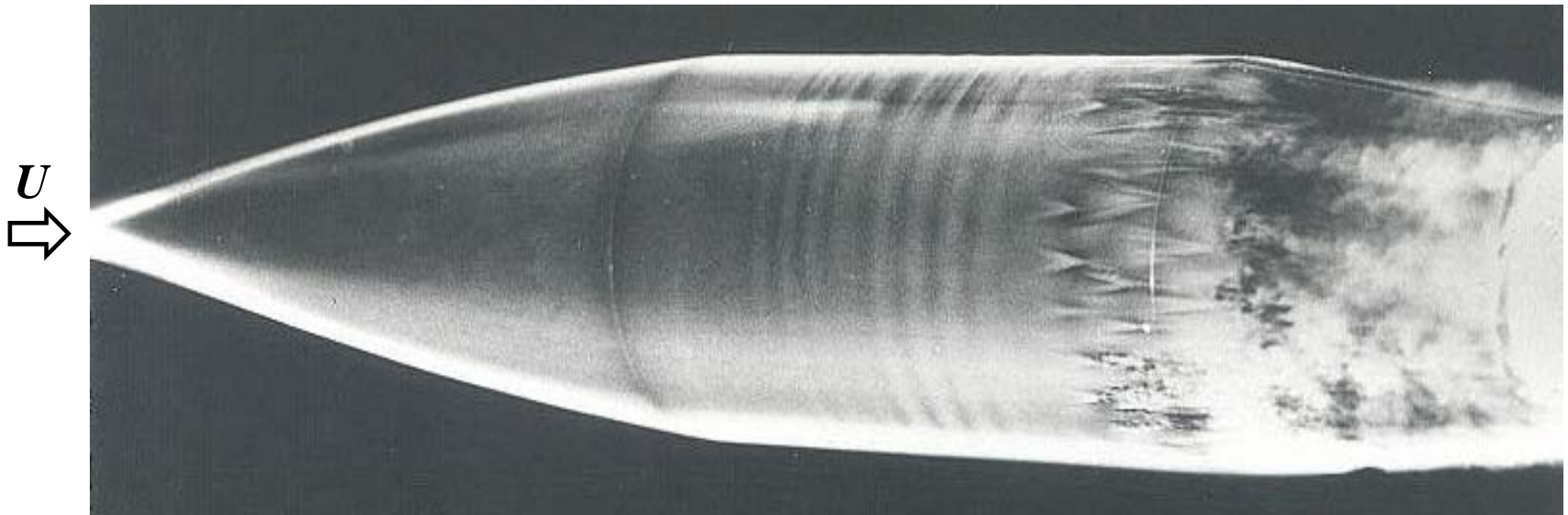


Position of boundary-layer instability onset (left) and transition (right) on a wing profile as function of chord Re number and lift coefficient c_l . A - boundary-layer separation for *laminar* flow until A; M - pressure minimum; S - stagnation point. For $Re_L \leq 5 \times 10^6$ transition occurs downstream of or around M.

- Experimental smoke visualization (snapshot) of TS-wave-induced breakdown on an axisymmetric body

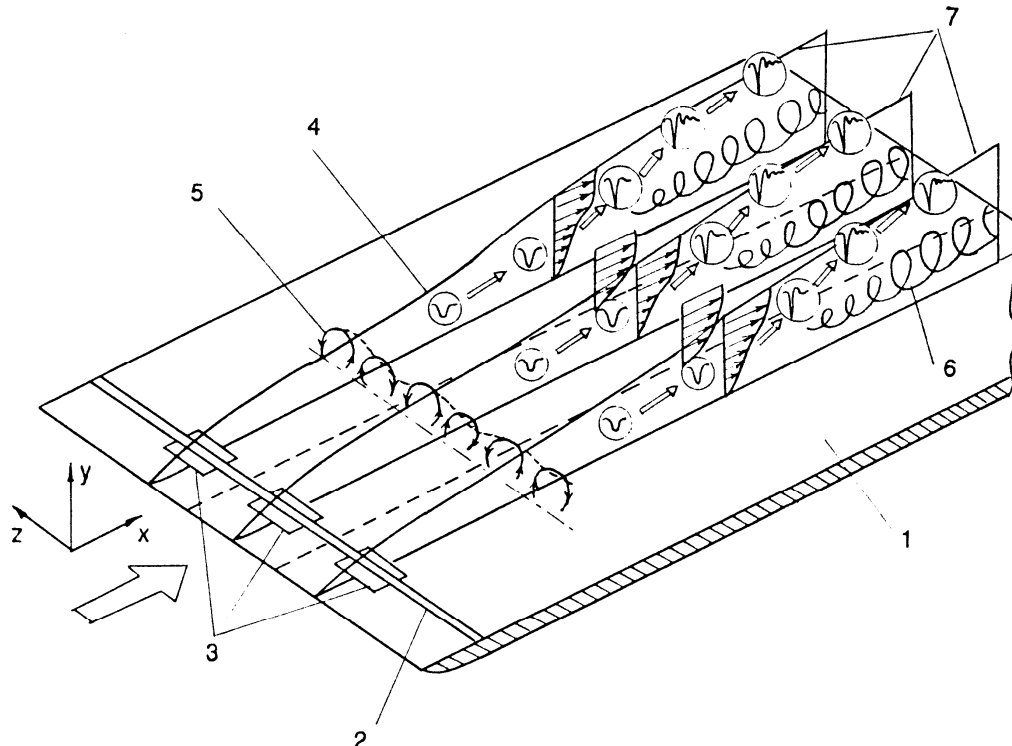
TS-waves

Λ -vortices



(T.J. Mueller, Nelson, Kegelmann, Morkovin 1981)

- Breakdown: Klebanoff's (1961) and Kachanov's (1985) controlled vibrating ribbon experiment in the Blasius boundary layer \Rightarrow K-Breakdown

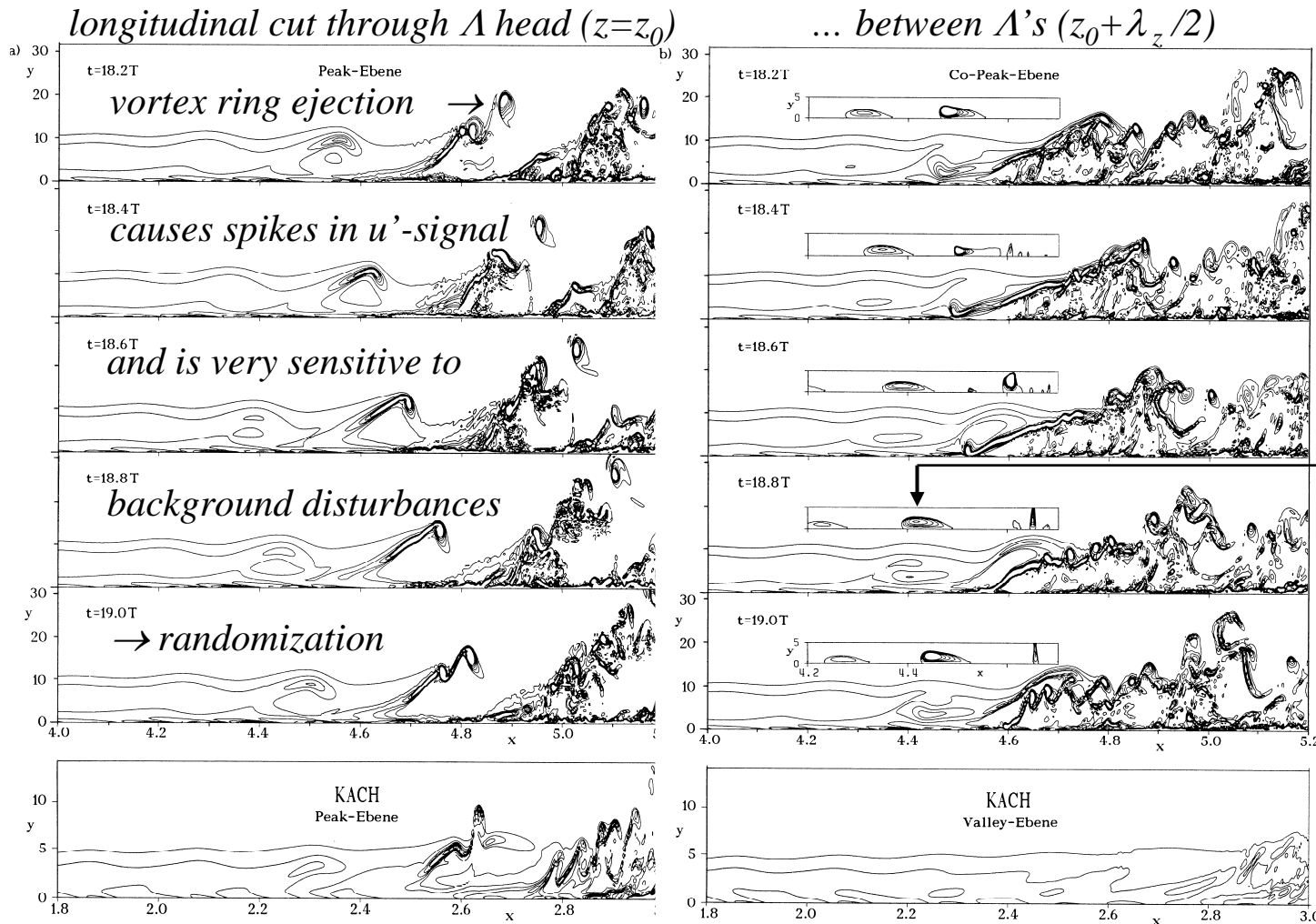


1 - plate, 2 - vibrating ribbon to induce 2-d Tollmien-Schlichting wave, 3 - tape spacers to prevent spanwise drift, 4 - boundary layer thickness, 5- longitudinal vortex pairs, 6 - turbulence start, 7 - disturbance "peak" planes with locally decelerated flow and instantaneous u-velocity "spike" signal

Scenario A – Breakdown (DNS, 1)

Flow Instability

- Details of K-Breakdown (with adverse pressure): spanwise vorticity / shear-layers

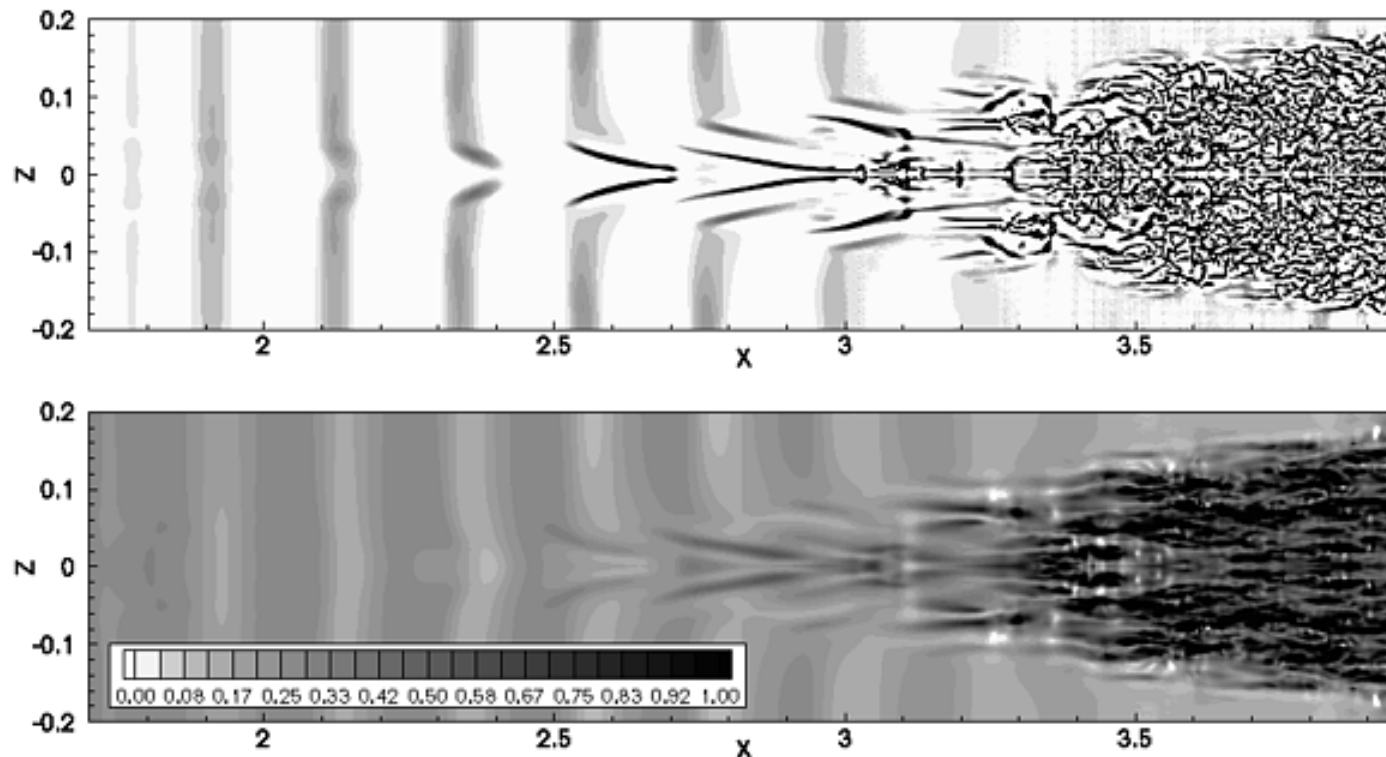


Snapshots during one fundamental time period

with downstream rolling separation zone due to large-amplitude 2-d TS wave in the decelerated Falkner-Skan-layer (not for Blasius flow)

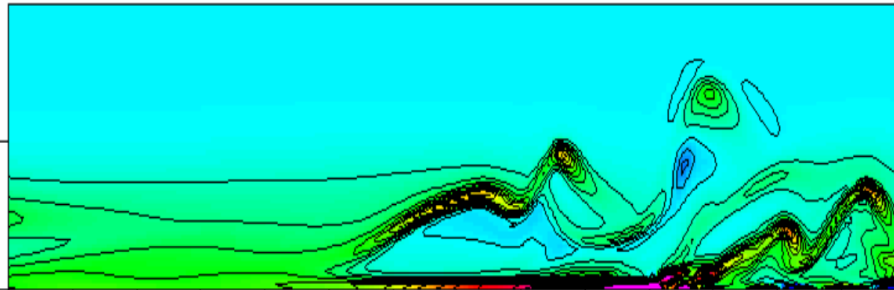
- Details of K-Breakdown with single tape strip: formation of Λ -vortex, top view, Blasius case. Single Λ -vortex induces side structures that break down independently

λ_2 -projection

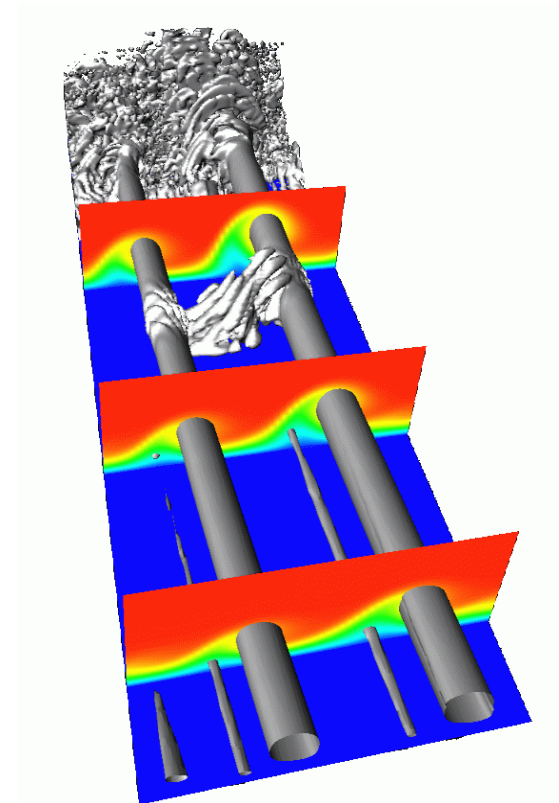


spanwise wall vorticity ~ friction
(z-symmetric DNS, D. Meyer 2002)

2-d boundary layer: hi-shear layer on Λ -vortex



2-d shear wake after a plate: vortex pairing



*3-d boundary layer:
crossflow-vortex
secondary instability*

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