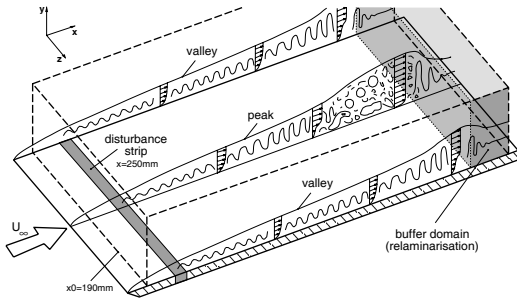


# Direct Numerical Simulation of Secondary $\Lambda$ -Vortices in a Transitional Boundary Layer

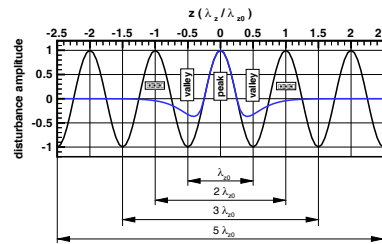
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## Integration Domain



- simulation of K-type breakdown using the full incompressible Navier-Stokes equations
- 2D Blasius baseflow ( $Re_{\delta_1}(x_0)=580$ )
- controlled disturbance generation by suction and blowing:
- 2D TS-wave (3-4%, 96.4 Hz) and 3D oblique waves generated by a steady modulation in spanwise direction
- disturbance waves grow downstream and give rise to the development of vortical structures in the flow field

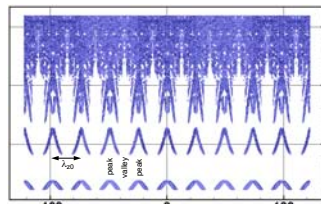
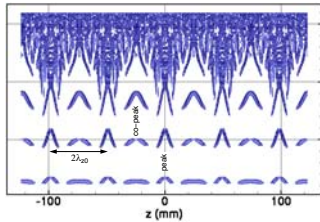
## Steady Spanwise Modulation of the TS-Wave



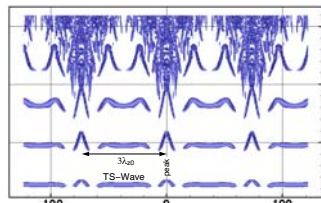
- comparison of periodic (black line) and local (blue line) modulations in spanwise direction allows to investigate whether  $\Lambda$ -structures can be generated by local or only by periodic disturbances
- simulation of more and more localized disturbances by increasing the width  $\lambda_z$  of the integration domain in spanwise direction in order to investigate the mutual influence of the vortical structures on each other:
- the idea is to move neighboring peak planes further apart of each other (basic width in periodically disturbed case:  $\lambda_z = \lambda_{z0} = 24.5 \text{ mm}$ )

## Vortex Visualization

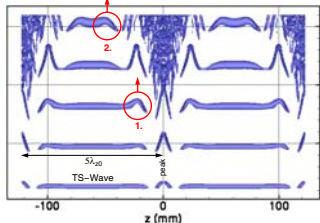
Periodic disturbance modulation in spanwise direction leads to a typical peak-valley splitting and the well known alignment of  $\Lambda$ -vortices for the K-type or fundamental breakdown process where  $\Lambda$ 's are formed side by side to each other.



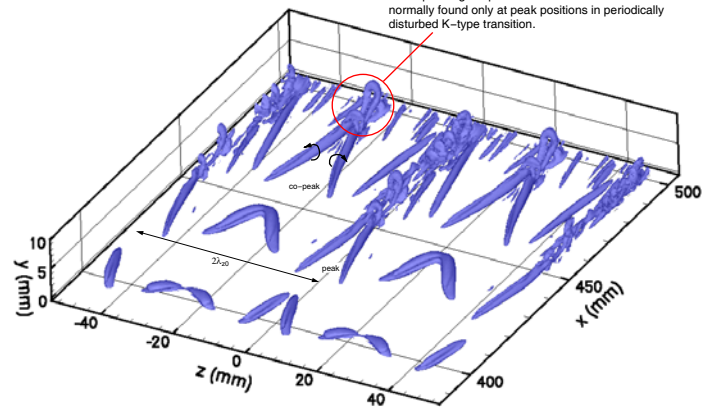
Side structures, called secondary structures in the following, emerge on each side of the  $\Lambda$ -vortices where they overlap and amplify each other forming a new peak plane (co-peak) with fully developed  $\Lambda$ 's further downstream at the expected valley positions.



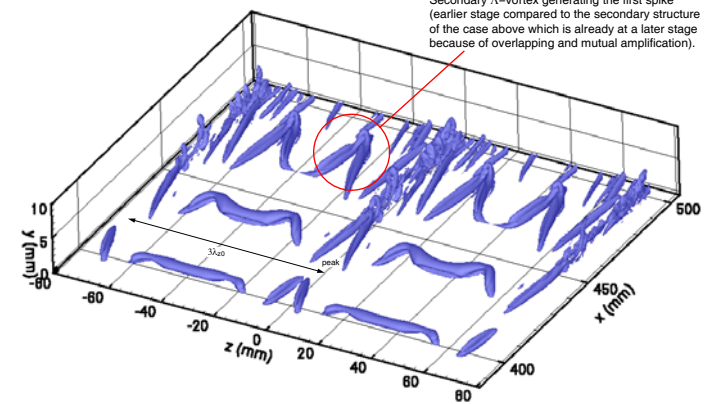
Secondary  $\Lambda$ -structures are stronger near to peak at first, they need some time until they become symmetric. This illustrates the local nature of the interaction of a  $\Lambda$ -vortex with the adjacent TS-wave which generates the secondary  $\Lambda$ 's. The remains of the large amplitude TS-wave can be seen between the peak planes as elongated structures.



Secondary  $\Lambda$ -structures produce even more secondary  $\Lambda$ 's by the same interaction process when they are fully developed, thus a cascade of new structures emerges away from peak initiating the following breakdown process.



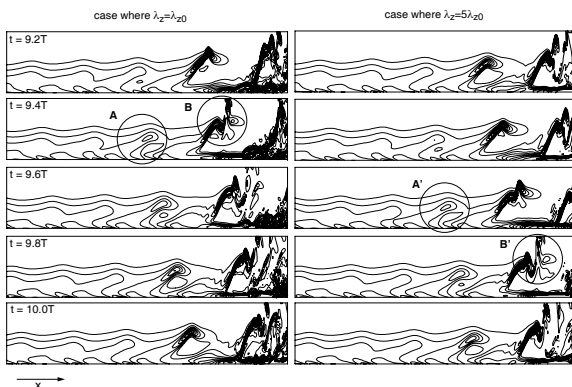
Fully developed secondary  $\Lambda$ -vortex at co-peak position with all expected features, especially ring-like vortices which generate strong negative velocity disturbances corresponding to spikes in timetraces of measurements - normally found only at peak positions in periodically disturbed K-type transition.



Secondary  $\Lambda$ -vortex generating the first spike (earlier stage compared to the secondary structure of the case above which is already at a later stage because of overlapping and mutual amplification).

## Vorticity component $\omega_z$ at peak position

## Conclusions



The process of formation of high-shear layers and spikes in the peak position is very similar in periodically (left) and locally (right) disturbed cases. The only difference is a slightly deferred development of these structures in the locally disturbed cases. This indicates that neighboring  $\Lambda$ -structures in the periodically disturbed case influence each other leading to higher amplification rates and an accelerated breakdown process compared to the locally disturbed cases.

- 1)  $\Lambda$ -vortices can be generated by periodic as well as by local disturbances in spanwise direction, despite the very different initial disturbance spectra the same structures evolve. Once formed from wave-like disturbances they can be considered as local structures which can overlap and amplify each other. They have a very strong influence on the surrounding fluid by an induction effect from the legs and the ring-like vortices.
- 2) The K-type breakdown process is independent of periodicity of disturbances in spanwise direction. Around the peak planes there is only a quantitative difference between locally and periodically disturbed cases (a slightly accelerated breakdown is observed in the latter case, because of mutual interaction of neighboring  $\Lambda$ 's), but the formation process of vortical structures, high-shear layers, and spikes is very similar in all cases. At off-peak positions also a qualitative difference can be observed, namely the formation of secondary  $\Lambda$ -vortices.
- 3) The newly found secondary  $\Lambda$ -vortices are generated by an interaction of an existing  $\Lambda$ -vortex with an adjacent TS-wave. This interaction consists of the combined effects of induction and of fluid displacement in spanwise direction away from and towards the peak plane caused by a  $\Lambda$ -structure when it passes a fixed downstream position. The TS-wave will be deformed this way and a new  $\Lambda$ -structure develops. This mechanism can generate a cascade of new secondary structures which then initiate the breakdown process downstream of their respective position. Experimental evidence exists that such secondary structures exist in actual transitional wall-bounded flows with local disturbances (Prof. Kachanov 1998, personal communication).